

1 解答

- [問 1] (a) 1
(b) 1
(c) 10

[問 2] $x = \frac{5 \pm \sqrt{13}}{2}, \frac{5 \pm \sqrt{3}i}{2}$

[問 3] (証明略)

2 解答

[問 1] $\vec{OP} = \frac{1}{3}\vec{a} + \frac{1}{3}\vec{b}$

[問 2] $\vec{OR} = \frac{t}{3t-1}\vec{b}$

[問 3] (a) $\frac{t^2}{3t-1}$

(b) 最大値 $\frac{1}{2}$ ($t = \frac{1}{2}, 1$), 最小値 $\frac{4}{9}$ ($t = \frac{2}{3}$)

3 解答

[問 1] $\left(\frac{2}{3}\right)^n$

[問 2] $\left(\frac{2}{3}\right)^n - \left(\frac{1}{2}\right)^n$

[問 3] $\frac{5^n - 2^{2n+1} + 3^n}{6^n}$

[問 4] $\frac{5^{n-1} - 2^{2n-1} + 3^{n-1}}{2 \cdot 6^{n-1}}$

4 解答

[問 1] (a) $\frac{\pi}{4}$

(b) $\log \sqrt{2}$

(c) $I_1 = \frac{\pi}{8} + \frac{\log \sqrt{2}}{2}, J_1 = \frac{\pi}{8} - \frac{\log \sqrt{2}}{2}$

[問 2] $I_n = \frac{\pi}{4(n^2+1)} + \frac{n}{(n^2+1)} \log \frac{\sqrt{2}(n+1)}{2}, J_n = \frac{n\pi}{4(n^2+1)} - \frac{1}{(n^2+1)} \log \frac{\sqrt{2}(n+1)}{2}$